## Inverse Projection

Computer Graphies Course, Fall 2023
Presenter: Hanh Le

## Inverse Projection



## Why Inverse Projection?

3D Reconstruction from Images

Gesture
Recognition

Depth Sensing in Consumer Electronics
Surveillance and Security Camera Calibration

Object Tracking
Robotics

## Augmented Reality

## Simulations and Virtual Environments

Medical Imaging

## 3D Reconstruction from Images

Using inverse projection to reconstruct threedimensional scenes from two-dimensional images.


## Augmented Reality



## Object Tracking

Using inverse projection to track the movement of objects in a video sequence.


## Medical Imaging

Using inverse projection to reconstruct three-dimensional images of internal structures from a series of 2D slices.


## Robotics

Using inverse projection to perceive and interact with their environment.


## Inverse Projection



Inverse Projection Transformation


## Inverse Projection Transformation



RGB image


Depth map

## Depth map



Data from DDAD Dataset. Left: Image. Middle: Disparity. Right: Uncertainty

## Depth estimation - Classical technique

## Stereo vision

## Depth estimation - Classical technique



## Depth estimation - Classical technique



## Depth estimation - Classical technique



## Depth estimation - Classical technique



## Depth estimation - Classical technique

## Stereo Setup

Correspondence Matching
Stereo vision

## Disparity Calculation

 Depth Calculation$$
\text { Depth }=\frac{\text { Baseline } \times \text { Focal Length }}{\text { Disparity }}
$$

## Depth Estimation - Deep learning methods

## MiDaS

## Structure from Motion

## Depth from Focus

## Inverse Projection



## Inverse Projection

4D homogeneous vector


## Inverse Projection

$$
P=\left[\begin{array}{cccc}
\frac{n}{r} & 0 & 0 & 0 \\
0 & \frac{n}{t} & 0 & 0 \\
0 & 0 & -\frac{f+n}{f-n} & -\frac{2 f n}{f-n} \\
0 & 0 & -1 & 0
\end{array}\right] \quad \Rightarrow \quad P^{-1}=\left[\begin{array}{cccc}
\frac{r}{n} & 0 & 0 & 0 \\
0 & \frac{t}{n} & 0 & 0 \\
0 & 0 & 0 & -1 \\
0 & 0 & \frac{f-n}{-2 f n} & \frac{f+n}{2 n}
\end{array}\right]
$$

- $n$ is the near clipping plane.
- $f$ is the far clipping plane.
- $r$ and $t$ are the right and top frustum values.


## Inverse Projection

$$
\left[\begin{array}{l}
x_{r} \\
y_{r} \\
z_{r} \\
w_{r}
\end{array}\right]=\left[\begin{array}{cccc}
\frac{n}{r} & 0 & 0 & 0 \\
0 & \frac{t}{n} & 0 & 0 \\
0 & 0 & 0 & -1 \\
0 & 0 & \frac{f-n}{-2 f n} & \frac{f+n}{2 n}
\end{array}\right] *\left[\begin{array}{c}
x \\
y \\
z \\
w
\end{array}\right]
$$

Inverse of perspective 4D homogeneous projection matrix
vector

## Inverse Projection

$$
\begin{aligned}
& {\left[\begin{array}{c}
x_{r} \\
y_{r} \\
z_{r} \\
w_{r}
\end{array}\right]=\left[\begin{array}{cccc}
\frac{n}{r} & 0 & 0 & 0 \\
0 & \frac{t}{n} & 0 & 0 \\
0 & 0 & 0 & -1 \\
0 & 0 & \frac{f-n}{-2 f n} & \frac{f+n}{2 n}
\end{array}\right] *\left[\begin{array}{c}
x \\
y \\
z \\
w
\end{array}\right]} \\
& \text { projection matrix } \\
& \text { vector } \\
& {\left[\begin{array}{l}
x_{r} \\
y_{r} \\
z_{r}
\end{array}\right]=\frac{1}{w_{r}}\left[\begin{array}{l}
x_{r} \\
y_{r} \\
z_{r}
\end{array}\right]}
\end{aligned}
$$



## Inverse Projection



## End.

Hope you enjoy!


